

# Bonus Exercises on Optical Sources and Detectors

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## Problem 1: Noise properties of photodetectors

The signal-to-noise ratio (SNR) is a measure of the quality of the detected signal. For a given detector bandwidth  $\Delta f$  the SNR can be calculated by relating the mean electrical signal power to the electrical noise power, which consists of shot noise and thermal noise from the load resistor  $R_L$ . For a PIN diode this results in:

$$SNR = \frac{\overline{i^2}}{\delta i^2} = \frac{(SP_e)^2}{2eSP_e\Delta f + \frac{4kT\Delta f}{R_L}}.$$

The quantity  $S$  denotes the responsivity for the detector,  $P_e$  the external optical power,  $kT$  the thermal energy, and  $\Delta f$  the electrical detection bandwidth. In the following we consider a photodiode which is specified with a responsivity of  $S = 0.95 \text{ A/W}$ . Perform the subsequent calculations for two different load resistors,  $R_L = 50 \Omega$  and  $R_L = 100 \text{ k}\Omega$ .

- Shot-noise-limited operation is obtained when the shot noise exceeds the thermal noise. Calculate the signal power that is necessary to obtain shot noise limited operation at room temperature.
- The bandwidth  $f_{\text{BW}}$  of a photodiode can be approximated by its  $RC$  time constant

$$f_{\text{BW}} = \frac{1}{2\pi R_L C}.$$

Calculate  $f_{\text{BW}}$  for a parasitic capacitance of  $C = 1 \text{ pF}$ . Which load resistance would you choose for highly sensitive and which one for high-speed detection?

- How does the SNR increase with  $P_e$  above and below the shot-noise limit. Sketch the SNR [dB] as a function of  $P_e$  [dBm].

## Questions and Comments:

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